

Calculation policy, KS1

The following pages show the progression in calculation (addition, subtraction, multiplication and division) and how this works in line with the National Curriculum. The consistent use of the CPA (concrete, pictorial, abstract) approach across the maths curriculum helps children develop mastery across all the operations in an efficient and reliable way. This policy shows how these methods develop children's confidence in their understanding of both written and mental methods.

KEY STAGE 1

Children develop the core ideas that underpin all calculation. They begin by connecting calculation with counting on and counting back, but they should learn that understanding wholes and parts will enable them to calculate efficiently and accurately, and with greater flexibility. They learn how to use an understanding of 10s and 1s to develop their calculation strategies, especially in addition and subtraction.

Key language: whole, part, ones, ten, tens, number bond, add, addition, plus, total, altogether, subtract, subtraction, find the difference, take away, minus, less, more, group, share, equal, equals, is equal to, groups, equal groups, times, multiply, multiplied by, divide, share, shared equally, times-table

Addition and subtraction: Children first learn to connect addition and subtraction with counting, but they soon develop two very important skills: an and effective calculation strategies based on known number bonds and an increasing awareness of place value. Addition and subtraction are taught in a way that is interlinked to highlight the link between the two operations.Multiplication and division: Children develop an awareness of equal groups and link this with tounting in equal steps, starting with 25, 5s and 10s. In Year 2, they learn to connect the language of equal groups with the mathematical symbols for multiplication and division.Fractions: In Year 1, these fractions; and learn to recognise equal stores, based on their number sense. For example, in Year 1, when faced with 15 – 3 and 15 – 13, they will adapt their ways of approaching the including obubles, and an understanding of the 2, 5 and 10 times-tables and how they are related to counting.Fractions: In Year 2, children encounter 1 wareness of equal groups and effective calculation are taught in a way to find the answer to the calculation. In this key stage, it is vital that children explore and experience a variety of strong images and manipulative representations of equal groups, including doubles, and an understanding of the 2, 5 and 10 times-tables and how they are related to counting.Fractions: In Year 2, children encounter 1 wareness of equal groups and effective calculation are taught in a way to find the answer to the calculation and division can be wepreince a variety of strong images and and any conserve and flexibility of approach, and the including doubles, and an understanding of the 2, 5 and 10 times-tables and how they are related to counting.Fractions: In Year 2, children encounter 1 wareness of equal groups including doubles, a	anding of esentations of amples and of equal unit fractions ney learn to
--	---

	Concrete	Pictorial	Abstract
Year 1 Addition	Counting and adding more Children add one more person or object to a group to find one more.	Counting and adding more Children add one more cube or counter to a group to represent one more.	Counting and adding more Use a number line to understand how to link counting on with finding one more.
			0 1 2 3 4 5 6 7 8 9 10
		One more than 4 is 5.	One more than 6 is 7. 7 is one more than 6.
			Learn to link counting on with adding more than one. 0 1 2 3 4 5 6 7 8 9 10 5 + 3 = 8
	Understanding part-part-whole relationship Sort people and objects into parts and understand the relationship with the whole.	Understanding part-part-whole relationship Children draw to represent the parts and understand the relationship with the whole.	Understanding part-part-whole relationship Use a part-whole model to represent the numbers. 10 6 46 $+$ 4 $=$ 10
	The parts are 2 and 4. The whole is 6.		6 + 4 = 10
	Knowing and finding number bonds within 10	Knowing and finding number bonds within 10	Knowing and finding number bonds within 10

Break apart a group and put back together to find and form number bonds. 3 + 4 = 7 6 = 2 + 4	Use five and ten frames to represent key number bonds. 5 = 4 + 1 $10 = 7 + 3$	Use a part-whole model alongside other representations to find number bonds. Make sure to include examples where one of the parts is zero. a) (4) $(0)(4)$ $(4)(4)$ (4)
Understanding teen numbers as a complete 10 and some more Complete a group of 10 objects and count more. <i>13 is 10 and 3 more.</i>	Understanding teen numbers as a complete 10 and some more Use a ten frame to support understanding of a complete 10 for teen numbers.	Understanding teen numbers as a complete 10 and some more. 1 ten and 3 ones equal 13. 10 + 3 = 13
Adding by counting on	Adding by counting on	Adding by counting on

Adding the 1s Children use bead strings to recognise how to add the 1s to find the total efficiently. $2+3=5$ $2+3=5$ $12+3=15$ Bridging the 10 using number bonds	Adding the 1s Children represent calculations using ten frames to add a teen and 1s. $2 + 3 = 5$ $12 + 3 = 15$ Bridging the 10 using number bonds	Adding the 1s Children recognise that a teen is made from a 10 and some 1s and use their knowledge of addition within 10 to work efficiently. 3 + 5 = 8 So, 13 + 5 = 18 Bridging the 10 using number bonds
Children use a bead string to complete a 10 and understand how this relates to the addition. 7 add 3 makes 10. So, 7 add 5 is 10 and 2 more.	Children use counters to complete a ten frame and understand how they can add using knowledge of number bonds to 10.	Use a part-whole model and a number line to support the calculation. 4 1 3 9 10 11 12 13 9 + 4 = 13

Subtraction	Children arrange objects and remove to find how many are left. 1 less than 6 is 5. 6 subtract 1 is 5.	Children draw and cross out or use counters to represent objects from a problem.	Children count back to take away and use a number line or number track to support the method. 876 $9-3=6$
	Finding a missing part, given a whole and a part Children separate a whole into parts and understand how one part can be found by subtraction. $\overrightarrow{}$ $\overrightarrow{}$	Finding a missing part, given a whole and a part Children represent a whole and a part and understand how to find the missing part by subtraction. 5 - 4 = 1	Finding a missing part, given a whole and a part Children use a part-whole model to support the subtraction to find a missing part. 7-3 = ? Children develop an understanding of the relationship between addition and subtraction facts in a part-whole model. - = = = = + = = = + = = = + = + = = + = + = = + = + = + = = + + = + = + + = + + = + + = + + = + + = + + = + + = + + = + + = + + = + + = + + = + + = + + + = + + + = + + + = + + + = + + + = + + + = + + + = + + + + = +
	Finding the difference	Finding the difference	Finding the difference

Arrange two groups so that the difference between the groups can be worked out.	Represent objects using sketches or counters to support finding the difference.	Children understand 'find the difference' as subtraction.
8 is 2 more than 6. 6 is 2 less than 8. The difference between 8 and 6 is 2.	5 - 4 = 1 The difference between 5 and 4 is 1.	10 - 4 = 6 The difference between 10 and 6 is 4.
Subtraction within 20 Understand when and how to subtract 1s efficiently.	Subtraction within 20 Understand when and how to subtract 1s efficiently.	Subtraction within 20 Understand how to use knowledge of bonds within 10 to subtract efficiently.
Use a bead string to subtract 1s efficiently. 5-3=2 15-3=12	Image: Constraint of the second state of the second sta	5 - 3 = 2 15 - 3 = 12
Subtracting 10s and 1s For example: 18 – 12	Subtracting 10s and 1s For example: 18 – 12	Subtracting 10s and 1s Use a part-whole model to support the calculation.
Subtract 12 by first subtracting the 10, then the remaining 2.	Use ten frames to represent the efficient method of subtracting 12.	
22222 2000 22222 2000		$ \begin{array}{c} 10 \\ 19 - 14 \\ 19 - 10 = 9 \end{array} $
First subtract the 10, then take away 2.	First subtract the 10, then subtract 2.	9 - 4 = 5 So, 19 - 14 = 5
Subtraction bridging 10 using number bonds	Subtraction bridging 10 using number bonds	Subtraction bridging 10 using number bonds

	For example: 12 – 7 Arrange objects into a 10 and some 1s, then decide on how to split the 7 into parts. 7 is 2 and 5, so I take away the 2 and then the 5.	Represent the use of bonds using ten frames.	Use a number line and a part-whole model to support the method. 13-5 (2) $(3)(-2)$ $(-3)(-2)$ $(-3)(-2)$ $(-3)(-3)(-3)$ $(-3)(-3)$ $(-3)(-3)$ (-3) $(-3)(-3)$ (-3) $($
Year 1 Multiplication	Recognising and making equal groups Children arrange objects in equal and unequal groups and understand how to recognise whether they are equal.	Recognising and making equal groups Children draw and represent equal and unequal groups.	Describe equal groups using words <i>Three equal groups of 4.</i> <i>Four equal groups of 3.</i>
	Finding the total of equal groups by counting in 2s, 5s and 10s There are 5 pens in each pack 510152025303540	Finding the total of equal groups by counting in 2s, 5s and 10s 100 squares and ten frames support counting in 2s, 5s and 10s.	Finding the total of equal groups by counting in 2s, 5s and 10s Use a number line to support repeated addition through counting in 2s, 5s and 10s.
Year 1	Grouping	Grouping	Grouping

Division	Learn to make equal groups from a whole and find how many equal groups of a certain size can be made. Sort a whole set people and objects into equal groups.	Represent a whole and work out how many equal groups.	Children may relate this to counting back in steps of 2, 5 or 10.
	Sharing Share a set of objects into equal parts and work out how many are in each part.	Sharing Sketch or draw to represent sharing into equal parts. This may be related to fractions. Image: Construction of the second seco	Sharing 10 shared into 2 equal groups gives 5 in each group.

	Year 2		
	Concrete	Pictorial	Abstract
Year 2 Addition			
Understanding 10s and 1s	Group objects into 10s and 1s.	Understand 10s and 1s equipment, and link with visual representations on ten frames.	Represent numbers on a place value grid, using equipment or numerals.
Adding 10s	Use known bonds and unitising to add 10s. ()) ()) ()) ()) ()) ()) ()) ()	Use known bonds and unitising to add 10s.	Use known bonds and unitising to add 10s. (4) (4) (3) (4+3= (4+3=7) (4+3=7) (4+3=7) (4+3=7) (4+3=7) (4+3=7) (4+3=7) (4+3=7) (4+3=7) (4+3=7) (4+3=7) (4+3=7) (4) (4) (5) (5) (5) (5) (5) (5) (5) (5

Adding a 1-digit number to a 2-digit number not bridging a 10	Add the 1s to find the total. Use known bonds within 10.	Add the 1s. 34 is 3 tens and 4 ones. 4 ones and 5 ones are 9 ones. The total is 3 tens and 9 ones. 1	Add the 1s. Understand the link between counting on and using known number facts. Children should be encouraged to use known number bonds to improve efficiency and accuracy. $30 \ 31 \ 32 \ 33 \ 34 \ 35 \ 36 \ 37 \ 38 \ 39 \ 40$ This can be represented horizontally or vertically. 34 + 5 = 39 or $\frac{1}{3} \ \frac{0}{4} \ \frac{1}{5} \ \frac{9}{9}$
Adding a 1-digit number to a 2-digit number bridging 10	Complete a 10 using number bonds.	Complete a 10 using number bonds.	Complete a 10 using number bonds. 7 5 2 43 44 45 46 47 48 49 50 51 52 53 $7 = 5 + 2$ $45 + 5 + 2 = 52$

Adding a 1-digit number to	Exchange 10 ones for 1 ten.	Exchange 10 ones for 1 ten.	Exchange 10 ones for 1 ten.
a 2-digit number using exchange			$\begin{array}{c} T \\ 2 \\ + \\ 1 \\ 1 \end{array}$
			T O 2 4 8 3 2 1
Adding a multiple of 10 to	Add the 10s and then recombine.	Add the 10s and then recombine.	Add the 10s and then recombine.
a 2-digit number		0 0	37 + 20 = ? 30 + 20 = 50 50 + 7 = 57
	27 is 2 tens and 7 ones. 50 is 5 tens.	\$\$\$\$\$\$	37 + 20 = 57
		66 is 6 tens and 6 ones. 66 + 10 = 76	
	There are 7 tens in total and 7 ones. So, 27 + 50 is 7 tens and 7 ones.	A 100 square can support this understanding.	

Adding a multiple of 10 to a 2-digit number using columns	Add the 10s using a place value grid to support. TODIENTIAL OPERATION OPERA	Add the 10s using a place value grid to support. TOOOOOOOOOOOOOOOOOOOOOOOOOOOOOOOOOOOO	Add the 10s represented vertically. Children must understand how the method relates to unitising of 10s and place value. $\begin{array}{r} \hline \\ \hline $
Adding two 2-digit numbers	Add the 10s and 1s separately. Add the 10s and 1s separately. 5+3=8 There are 8 ones in total. 3+2=5 There are 5 tens in total. 35+23=58	Add the 10s and 1s separately. Use a part-whole model to support. 32 + 11 + 132 + 10 + 1 $32 + 10 = 42$ $42 + 1 = 43$ $32 + 11 = 43$	Add the 10s and the 1s separately, bridging 10s where required. A number line can support the calculations. $\underbrace{+10 + 10 + 3 + 2}_{17} + \underbrace{10}_{17} + \underbrace{2.5}_{17}$ $17 + 25$

Adding two 2-digit numbers	Add the 1s. Then add the 10s.		Add the 1s. Then add the 10s.
using a place value grid	Tens Ones		$\begin{array}{c} T \\ \hline 0 \\ \hline 3 \\ + \\ 1 \\ \hline 6 \end{array}$
	+		T O 3 2 + 1 4 4 6
Adding two	Add the 1s. Exchange 10 ones for a ten. Then add the 10s	47 + 25	Add the 1s. Exchange 10 ones for a ten. Then
2-digit numbers with exchange	add the 10s. Tens Ones Ones Tens <	$+ \qquad \qquad$	add the 10s. $\frac{1}{3} \frac{0}{6} + \frac{2}{5} \frac{0}{1}$ $\frac{1}{3} \frac{0}{6} + \frac{2}{5} \frac{0}{5}$

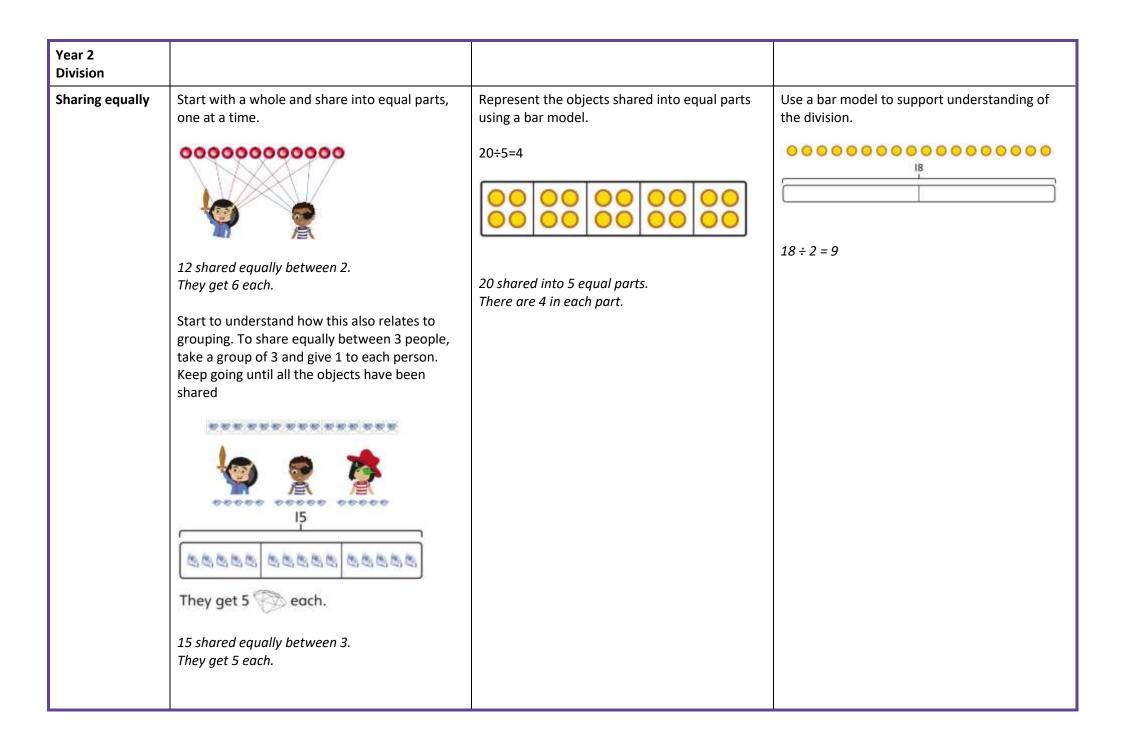
Year 2 Subtraction			
Subtracting multiples of 10	Use known number bonds and unitising to subtract multiples of 10.	Use known number bonds and unitising to subtract multiples of 10.	Use known number bonds and unitising to subtract multiples of 10.
	CONTRACTOR OF STATES OF ST	100 30	2 5 20 50
	8 subtract 6 is 2. So, 8 tens subtract 6 tens is 2 tens.	10 − 3 = 7 So, 10 tens subtract 3 tens is 7 tens.	7 tens subtract 5 tens is 2 tens. 70 – 50 = 20
Subtracting a single-digit number	Subtract the 1s. This may be done in or out of a place value grid.	Subtract the 1s. This may be done in or out of a place value grid.	Subtract the 1s. Understand the link between counting back and subtracting the 1s using known bonds. 30 31 32 33 34 35 36 37 38 39 40
			$ \begin{array}{cccc} T & O \\ \overline{3} & 9 \\ - & 3 \\ \overline{3} & 6 \\ \overline{39 - 3} = 6 \\ \overline{39 - 3} = 36 \end{array} $
Subtracting a single-digit	Bridge 10 by using known bonds.	Bridge 10 by using known bonds.	Bridge 10 by using known bonds.
number bridging 10			-4 -4 16 17 18 19 20 21 22 23 24 25 26
	35 – 6 I took away 5 counters, then 1 more.	35 – 6 First, I will subtract 5, then 1.	24 - 6 = ? 24 - 4 - 2 = ?

Subtracting a single-digit number using exchange	Exchange 1 ten for 10 ones. This may be done in or out of a place value grid.	Exchange 1 ten for 10 ones.	Exchange 1 ten for 10 ones. TO 'Z'5 - 7 8 TO Z'5 - 7 8 25 - 7 = 18
Subtracting a 2-digit number	Subtract by taking away.	Subtract the 10s and the 1s. This can be represented on a 100 square. 1 2 3 4 5 6 7 8 9 10 1 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100	Subtract the 10s and the 1s. This can be represented on a number line. 40 - 10 - 10 - 10 - 10 - 10 - 10 - 10 -

Subtracting a 2-digit number using place value and columns	Subtract the 1s. Then subtract the 10s. This may be done in or out of a place value grid. T O O O O O O O O O O O O O O O O O O O	Subtract the 1s. Then subtract the 10s.	Using column subtraction, subtract the 1s. Then subtract the 10s. TO 4 5 - 1 2 3 TO 4 5 - 1 2 3 3
Subtracting a 2-digit number with exchange		Exchange 1 ten for 10 ones. Then subtract the 1s. Then subtract the 10s. Take 16 away from 34 34 - 16 = 30 and 4. That can become 20 and 14, then we can take away 16 easily!	Using column subtraction, exchange 1 ten for 10 ones. Then subtract the 1s. Then subtract the 10s. $\frac{T}{4} \frac{O}{4} \frac{O}{5}$ $-\frac{2}{2} \frac{7}{7}$ $\frac{T}{3} \frac{O}{3} \frac{1}{4} \frac{1}{5}$ $-\frac{2}{2} \frac{7}{7}$ $\frac{T}{8} \frac{O}{3} \frac{1}{4} \frac{1}{5}$ $-\frac{2}{2} \frac{7}{7}$ $\frac{8}{1} \frac{T}{8}$

Year 2 Multiplication			
Equal groups and repeated addition	Recognise equal groups and write as repeated addition and as multiplication.	Recognise equal groups using standard objects such as counters and write as repeated addition and multiplication.	Use a number line and write as repeated addition and as multiplication. $\begin{array}{c} & & \\$
Using arrays to represent multiplication and support understanding	Understand the relationship between arrays, multiplication and repeated addition.	Understand the relationship between arrays, multiplication and repeated addition.	Understand the relationship between arrays, multiplication and repeated addition. $\begin{array}{c} & & \\ & & \\ & & \\ 0 & 5 & 10 & 15 & 20 & 25 \\ & & 5 \times 5 = 25 \end{array}$
Understanding commutativity	Use arrays to visualise commutativity.	Form arrays using counters to visualise commutativity. Rotate the array to show that orientation does not change the multiplication.	Use arrays to visualise commutativity. $4+4+4+4+4=20$ $5+5+5=20$ $4 \times 5 = 20 \text{ and } 5 \times 4 = 20$

Learning ×2, ×5 and ×10 table facts	Develop an understanding of how to unitise groups of 2, 5 and 10 and learn corresponding times-table facts.	Understand how to relate counting in unitised groups and repeated addition with knowing key times-table facts.	Understand how the times-tables increase and contain patterns.
		000000000	
		000000000	
	5.5 E	0 10 20 30	
	3 groups of 10 10, 20, 30 3 × 10 = 30	10 + 10 + 10 = 30 $3 \times 10 = 30$	
			10 10 10 10 10 10 10 10 10 10 10 10 10 1
			10 10 10 10 10 10 10 10 10 10 10 10 10 1
			6 × 10 = 60



Grouping equally	Understand how to make equal groups from a whole.	Understand the relationship between grouping and the division statements.	Understand how to relate division by grouping to repeated subtraction.
	<u></u>	$12 \div 3 = 4$	
	8 divided into 4 equal groups. There are 2 in each group.	12 ÷ 4 = 3	0 1 2 3 4 5 6 7 8 9 10 11 12
	8÷4=2		There are 4 groups now.
		12 ÷ 2 = 6	12 divided into groups of 3. $12 \div 3 = 4$
			There are 4 groups.
Using known times-tables to solve divisions	Understand the relationship between multiplication facts and division.	Link equal grouping with repeated subtraction and known times-table facts to support division.	Relate times-table knowledge directly to division.
		40 divided by 4 is 10.	$I \times 10 = 10$ $2 \times 10 = 20$ $3 \times 10 = 30$ $4 \times 10 = 40$ $5 \times 10 = 50$ $6 \times 10 = 60$ $7 \times 10 = 70$ $S \times 10 = 90$ $I used the 10 times-table to help me. 3 \times 10 = 30.$
	4 groups of 5 cars is 20 cars in total. 20 divided by 4 is 5.	Use a bar model to support understanding of the link between times-table knowledge and division.	8 × 10 = 80 I know that 3 groups of 10 makes 30, so I know that 30 divided by 10 is 3.
		60 10 10	3 × 10 = 30 so 30 ÷ 10 = 3